

**Engineering Paper 1**

1. The base quantity among the following is

- (a) Speed
- (b) Weight
- (c) Length
- (d) Area

Answer: c

Solution

There are seven base quantities, (i) Mass (ii) Length (iii) Time (iv) Current (v) Amount of substance (vi) Luminous intensity (vii) Temperature

2. Which of the following is not a unit of time?

- (a) Second
- (b) Minute
- (c) Hour
- (d) Light year

Answer: d

Solution

Light year is the unit of distance. 1 light year =  $9.46 \times 10^{15}m$

3. One astronomical unit is a distance equal to

- (a)  $9.46 \times 10^{15}m$
- (b)  $1.496 \times 10^{11}m$
- (c)  $3 \times 10^8m$
- (d)  $3.08 \times 10^{16}m$

Answer: b

Solution

One astronomical unit is the average distance between earth and sun. 1 astronomical unit (AU) =  $1.496 \times 10^{11}m$

4. The volume of a cube having sides 1.2 m is appropriately expressed as

- (a)  $1.728 \times 10^6 cm^3$
- (b)  $1.7 \times 10^6 cm^3$
- (c)  $1.8 \times 10^6 cm^3$
- (d)  $1.73 \times 10^6 cm^3$

Answer: b

Solution

The volume of cube is

$$v = (1.2cm)^3 = 1.728 \times 10^6 cm^3$$

$$v \simeq 1.7 \times 10^6$$

. Answer should be reported in minimum number of significant figures

5. Ampere second is a unit of

- (a) Current
- (b) Charge
- (c) Energy
- (d) Power

Answer: b

Solution

$$\text{Current } I = \frac{q}{t} \Rightarrow q = It$$

$$q = \text{Ampere second}$$

So, ampere second is the unit of charge.

6. The most precise reading of the mass of an object, among the following is

- (a) 20 g
- (b) 20.0 g
- (c) 20.01 g
- (d)  $20 \times 10^0g$

Answer: c

Solution

A measurement having more number of decimal places is the one with the most precision. So, 20.01 g is most precise.

7. The most accurate reading of the length of a 6.28 cm long fibre is

- (a) 6 cm
- (b) 6.5 cm
- (c) 5.99 cm
- (d) 6.0 cm

Answer: b

Solution

Most accurate reading is the one having minimum error. So,

$$16 - 6.281 = 0.28cm$$

$$16.5 - 6.281 = 0.22cm$$

$$15.99 - 6.281 = 0.29cm$$

$$16.0 - 6.281 = 0.28cm$$

So, second reading is most accurate.

8. Which of the following is a unit that of force?

- (a) N m
- (b) mN
- (c) nm
- (d) N s

Answer: b

Solution

$$Nm \rightarrow \text{Unit of torque}$$

$$mN \rightarrow \text{Milli newton} \Rightarrow 10^{-3}N$$

$$nm \rightarrow \text{Nano metre}$$

$$Ns \rightarrow \text{Unit of momentum}$$

9. The total plane angle subtended by a circle at its centre is

- (a)  $\pi$  rad
- (b)  $2\pi$  rad
- (c)  $\frac{2\pi}{3}$  rad
- (d)  $\frac{\pi}{2}$  rad

Answer: b

Solution

The total plane angle is  $360^\circ$  or  $2\pi$  rad

10. One unified atomic mass unit represents a mass of magnitude

- (a)  $10^{-30}$  kg
- (b)  $1.66 \times 10^{27}$  kg
- (c)  $1.66 \times 10^{-27}$  kg
- (d)  $10^{30}$  kg

Answer: c

Solution

$$1 \text{ amu} = 1.66 \times 10^{-27} \text{ kg}$$

11. Which of the following does not possess the same dimensions as that of pressure?

- (a) Stress
- (b) Bulk modulus
- (c) Thrust
- (d) Energy density

Answer: c

12. The dimensional formula for thermal resistance is
- $[ML^2T^{-3}K^{-1}]$
  - $[ML^2T^{-2}A^{-1}]$
  - $[ML^2T^{-3}K^{-2}]$
  - $[M^{-1}L^2T^3K]$
- Answer:** d
13. The units of length; velocity and force are doubled. Which of the following is the correct change in the other units
- Unit of time is doubled
  - Unit of mass is doubled
  - Unit of momentum is doubled
  - Unit of energy is doubled
- Answer:** c

14. Which one of the following is not the dimensionless quantity?
- Plancks constant
  - Dielectric constant
  - Solid angle
  - Strain
- Answer:** a

15. The dimensions of impulse are equal to that of
- force
  - linear momentum
  - pressure
  - angular momentum
- Answer:** b

16. The dimensions of the ratio of angular to linear momentum is
- $[M^0LT^0]$
  - $[MLT^{-1}]$
  - $[ML^2T^{-1}]$
  - $[M^{-1}L^{-1}T^{-1}]$
- Answer:** a

17. The dimensional representation of specific resistance in terms of charge Q is
- $[ML^3T^{-1}Q^{-2}]$
  - $[ML^2T^{-2}Q^2]$
  - $[MLT^{-2}Q^{-1}]$
  - $[ML^2T^{-2}Q^{-1}]$
- Answer:** a

18. Out of the following four dimensional quantities; which one qualifies to be called a dimensional constant?
- Acceleration due to gravity
  - Surface tension of water
  - Weight of a standard kilogram mass
  - The velocity of light in vacuum
- Answer:** d

19. On measuring electric energy; 1 kWh is equal to
- $3.6 \times 10^4 J$
  - $3.6 \times 10^6 J$
  - $7.3 \times 10^6 J$
  - None of these
- Answer:** b

20.  $ML^{-1}T^{-1}$  stand for dimensions of
- work
  - torque
  - linear momentum
  - coefficient of viscosity
- Answer:** a

21. Haemoglobin contains 0.334% of iron by weight. The molecular weight of haemoglobin is approximately 67200. The number of iron atoms at (at weight of Fe is 56) present in one molecule of haemoglobin are
- 1
  - 6
  - 4
  - 2
- Answer:** c

22. If the uncertainty in the position of electron is zero, the uncertainty in its momentum would be
- zero
  - greater than  $\frac{h}{4}\pi$
  - less than  $\frac{h}{4}\pi$
  - infinite
- Answer:** d

**Solution**

$$\Delta p = \frac{h}{4\pi\Delta x} = \frac{h}{4\pi \times zero} = \infty \text{ (infinite)}$$

23. What mass of  $H_2(g)$  is needed to reduce 192gm. of  $MoO_3$  to metal? [At wt. of Mo=96]
- 8gm
  - 16gm
  - 32gm
  - None of these
- Answer:** a

**Solution**

$$\text{Equivalent of } MoO_3 = \frac{M}{6} = \frac{144}{6} = 24$$

$$\text{equivalent of } H_2 : \frac{192}{24} = \frac{W_{H_2}}{1} \Rightarrow W_{H_2} = 8gm.$$

24. If  $E_1, E_2$ ; and  $E_3$  represents respectively the kinetic energies of an electron and an alpha particle and a proton each having same de brogile wavelength then
- $E_1 > E_3 > E_2$
  - $E_2 > E_3 > E_1$
  - $E_1 > E_2 > E_3$
  - $E_1 = E_2 = E_3$
- Answer:** a

**Solution**

Since K.E. =  $\frac{1}{2}mv^2$  and  $\lambda = \frac{h}{mv}$ .

$$\therefore K.E. = \frac{1}{2}m \cdot \frac{h^2}{m^2\lambda^2} = \frac{h^2}{2m\lambda^2}. \text{ As } \lambda \text{ is the same.}$$

$$\therefore K.E. \propto \frac{1}{m}$$

25. The shortest wavelength of the line in hydrogen atomic spectrum of Lyman series when  $R_H = 109678cm^{-1}$  is
- 1002.7  $\text{\AA}$
  - 1215.67  $\text{\AA}$
  - 1127.30  $\text{\AA}$
  - 911.7  $\text{\AA}$
- Answer:** a

**Solution**

$$\bar{\nu} = \frac{1}{\lambda} = R_H \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

For Lyman series,  $n_1 = 1$  and  $n_2 = \infty$

$$\text{then, } \frac{1}{\lambda} = R_H \left( \frac{1}{(1)^2} - \frac{1}{\infty} \right)$$

$$\text{or, } \lambda = \frac{1}{R_H} \text{ or } \lambda = \frac{1}{109678}$$

$$= 911.7 \times 10^{-8} \text{ cm} = 911.7 \text{\AA}$$

26. The work function of a metal is 5 eV. what is the kinetic energy of the photoelectron ejected from the metal surface if the energy of the incident radiation is 6.2 eV? ( $1\text{eV} = 1.6 \times 10^{-19}\text{J}$ )

- (a)  $6.626 \times 10^{-19}\text{J}$
- (b)  $8.01 \times 10^{-19}\text{J}$
- (c)  $1.92 \times 10^{-18}\text{J}$
- (d)  $8.010 \times 10^{-18}\text{J}$

Answer: c  
Solution

$$K.E. = h\nu - h\nu_0 = 6.2 - 5.0 = 1.2\text{eV}$$

$$1\text{eV} = 1.6 \times 10^{-19}\text{J}$$

$$\text{then } 1.2\text{eV} = 1.2 \times 1.6 \times 10^{-19}\text{J}$$

$$= 1.92 \times 10^{-19}\text{J}$$

27. The maximum number of molecules is present in

- (a) 15 L of  $\text{H}_2$  gas at STP
- (b) 5 L of  $\text{N}_2$  gas at STP
- (c) 0.5 g of  $\text{H}_2$  gas
- (d) 10 g of  $\text{O}_2$  gas

Answer: a  
Solution

No. of molecules in different cases

$$\begin{aligned} \text{(a) } \therefore 22.4 \text{ litre at STP contains} \\ = 6.023 \times 10^{23} \text{ molecule of } \text{H}_2 \\ \therefore 15 \text{ litre at STP contains} \end{aligned}$$

$$= \frac{15}{22.4} \times 6.023 \times 10^{23}$$

$$\begin{aligned} \text{(b) } \therefore 22.4 \text{ litre at STP contains} \\ = 6.023 \times 10^{23} \text{ molecule of } \text{N}_2 \end{aligned}$$

$$\therefore 5 \text{ litre at STP contains} = \frac{5}{22.4} \times 6.023 \times 10^{23}$$

$$\text{(c) } \therefore 2 \text{ gm of } \text{H}_2 = 6.023 \times 10^{23} \text{ molecules of } \text{H}_2$$

$$\therefore 0.5 \text{ gm of } \text{H}_2 = \frac{0.5}{2} \times 6.023 \times 10^{23}$$

$$\begin{aligned} \text{(d) Similarly } 10\text{g of } \text{O}_2 \text{ gas} \\ = \frac{10}{32} \times 6.023 \times 10^{23} \text{ molecules} \end{aligned}$$

Thus (a) will have maximum number of molecules

28. The vapour density of a gas is 11.2 then 11.2 g of this gas at N.T.P. will occupy a volume

- (a) 11.2L
- (b) 22.4L
- (c) 11.2mL
- (d) 22.4mL

Answer: a  
Solution

Vapour density of any gas occupies a volume of 11.2 litre at N.T.P.

29. Which of the following sets of quantum numbers represents the highest energy of atom?

- (a)  $n=3; l=0 m=0 s=+1/2$
- (b)  $n=3; l=1 m=1 s=+1/2$
- (c)  $n=3; l=2 m=1 s=+1/2$
- (d)  $n=4; l=0 m=0 s=+1/2$

Answer: c  
Solution

(a)  $n=3, l=0$  means 3s-orbital and  $n+1=3$

(b)  $n=3, l=1$  means 3p-orbital  $n+1=4$

(c)  $n=3, l=2$  means 3d-orbital  $n+1=5$

(d)  $n=4, l=0$  means 4s-orbitl  $n+1=4$

Increasing order of energy among these orbitals is

$$3s < 3p < 4s < 3d$$

$\therefore$  3d has highest energy

30. A binary compound of elements X and Y contains 50% of X. If the atomic masses of X and Y are 10 and 20 and the molecular mass of the compound is 120, the molecular formula of the compound is

- (a)  $\text{X}_2$
- (b)  $\text{X}_4\text{Y}_2$
- (c)  $\text{X}_6\text{Y}_3$
- (d)  $\text{X}_3\text{Y}_2$

Answer: c  
Solution

$$\text{X} \rightarrow \frac{50}{10} = 5 \rightarrow 2, \text{ simple ratio } \text{Y} \rightarrow \frac{50}{20} = 2.5 \rightarrow 1, \text{ simple ratio}$$

$$\text{Empirical formula} = \text{X}_2\text{Y} \text{ Empirical formula mass} = 40 \text{ n} = \frac{120}{40} = 3$$

$$\text{M.F} = (\text{E. F})_3 = \text{X}_6\text{Y}_3$$

31. The molecular formula of a compound is  $\text{M}_6\text{O}_1$ . If 20g of the compound contains 9g of the metal, atomic mass of the metal is

- (a) 40
- (b) 36
- (c) 28
- (d) 24

Answer: d  
Solution

$$\text{Atomic mass of the metal} = \text{X } 6x / (6x + 11 \times 16) = 9/20 \text{ X} = (9 \times 11 \times 16 / 11 \times 6) = 24$$

32. Which of the following at STP contains largest number of atoms?

- (a)  $800\text{cm}^3$  of  $\text{O}_2$
- (b)  $500\text{cm}^3$  of  $\text{NH}_3$
- (c)  $600\text{cm}^3$  of  $\text{SO}_2$
- (d)  $700\text{cm}^3$  of  $\text{O}_3$

Answer: d  
Solution

$$\text{Number of atoms From A.} = \frac{2 \times 800}{22400} \times 6.022 \times 10^{23} \text{ From B.} =$$

$$\frac{3 \times 500}{22400} \times 6.022 \times 10^{23} \text{ From C.} = \frac{3 \times 600}{22400} \times 6.022 \times 10^{23} \text{ From D.} = \frac{3 \times 700}{22400} \times 6.022 \times 10^{23}$$

33. At STP, volume of 0.01g of  $\text{H}_2$  is the same as that of

- (a) 0.22g of  $\text{CO}_2$
- (b) 0.085g of  $\text{NH}_3$
- (c) 0.32g of  $\text{SO}_2$
- (d) all of these

Answer: d  
Solution

$$\text{Volume of } 0.01\text{g of } \text{H}_2 \text{ at STP} = \frac{0.01}{2} \times 22.414\text{L} \text{ Volume of } 0.22\text{g}$$

$$\text{of } \text{CO}_2 = \frac{0.22}{44} \times 22.414\text{L} \text{ Volume of } 0.085\text{g of } \text{NH}_3 = \frac{0.085}{17}$$

$$\times 22.414\text{L} \text{ Volume of } 0.32\text{g of } \text{SO}_2 = \frac{0.32}{64} \times 22.414\text{L}$$

34.  $6.022 \times 10^{20}$  molecules of urea are present in 100ml of its solution. The concentration of urea solution is

- (a) 0.001 M
- (b) 0.01 M
- (c) 0.02 M
- (d) 0.1 M

Answer: b  
Solution

$$\text{No of moles of urea} = \frac{6.022 \times 10^{20}}{6.022 \times 10^{23}} = 0.001\text{mol} \text{ Concentration of}$$

$$\text{solution} = \frac{W_B}{M_B} \times \frac{1000}{V_{mL}} = 0.001\text{mol} \times \frac{1000}{100\text{L}} = 0.01\text{molL}^{-1} = 0.01\text{M}$$

35. No of  $H_2O$  molecules in a drop of water weighing 0.05g is:

- (a)  $1.5 \times 10^{23}$
- (b)  $1.672 \times 10^{21}$
- (c)  $1.5 \times 10^{20}$
- (d)  $6.022 \times 10^{22}$

Answer: b

Solution

1.80g of  $H_2O$  contain molecules =  $6.022 \times 10^{23}$  0.05g of  $H_2O$

$$\text{contain molecules} = \frac{(0.05g)}{(18.0g)} \times 6.022 \times 10^{23} = 1.672 \times 10^{21}$$

$$\text{molecules} = 1.672 \times 10^{21}$$

36. Maximum number of electrons in a subshell of an atom is determined by the following

- (a)  $2l + 1$
- (b)  $4l + 1$
- (c)  $2n^2$
- (d)  $4l + 2$

Answer: d

Solution

For a given value of l, maximum number of electrons in a subshell =  $2(2l + 1) = 4l + 2$

37. Bohr's radius for the H -atom ( n = 1) is approximately 0.53 Ampere. The radius of the first excited state ( n = 2) is

- (a) 0.13 A
- (b) 1.06 A
- (c) 4.77 A
- (d) 2.12 A

Answer: d

Solution

The radius of first excited state orbit ( n = 2) =  $0.53 \text{ A} \times 4 = 2.12 \text{ A}$

38. The following quantum number are possible for how many orbitals? ( n = 3, l = 2, m = +2)

- (a) 1
- (b) 2
- (c) 3
- (d) 4

Answer: a

Solution

m = +2 represents only one orbital

39. The value of Planck's constant is  $6.63 \times 10^{-34}$  Js. The velocity of light is  $3.0 \times 10^8 \text{ ms}^{-1}$ . Which value of closest to the wavelength in nanometers of a quantum of light with frequency of  $8 \times 10^{15} \text{ s}^{-1}$ ?

- (a)  $2 \times 10^{-25}$
- (b)  $5 \times 10^{-18}$
- (c)  $4 \times 10^1$
- (d)  $3 \times 10^7$

Answer: c

Solution

$$\text{According to wave theory } \lambda = \frac{c}{\nu} = \frac{(3 \times 10^8 \text{ ms}^{-1})}{8 \times 10^{15} \text{ s}^{-1}} =$$

$$37.5 \times 10^{-9} \text{ m} = 37.5 \text{ nm} = 4 \times 10^1$$

40. Which of the following represents the electron probability function (D)?

- (a)  $4\pi r dr \Psi^2$
- (b)  $4\pi r^2 dr \Psi$
- (c)  $4\pi r^2 dr \Psi^2$
- (d)  $4\pi r dr \Psi$

Answer: c

Solution

Electron probability function is  $4\pi r^2 dr \Psi^2$

41. The range of the function  $\sin(\sin^{-1} x + \cos^{-1} x)$ ,  $|x| \leq 1$  is

- (a) [-1, 1]
- (b) [1, -1]
- (c) {0}
- (d) {1}

Answer: d

Solution

$$\text{gof} = g(f(x)) = g(x^2) = x^2 + 5$$

42. Let  $f: R \rightarrow R: f(x) = x^2$  and  $g: R \rightarrow R: g(x) = x + 5$  then gof is:

- (a) ( x+5)
- (b) ( x+5<sup>2</sup>)
- (c) ( x<sup>2</sup>+5<sup>2</sup>)
- (d) (x<sup>2</sup> + 5)

Answer: d

Solution

$$R = \{(a, b) : 1 + ab > 0\}$$

It is clear that the given relation on S is reflexive, symmetric but not transitive.

43. Let S be the set of all real numbers. Then the relation  $R = \{(a, b) : 1 + ab > 0\}$  on S is

- (a) reflexive and symmetric but not transitive
- (b) reflexive and transitive but not symmetric
- (c) symmetric and transitive but not reflexive
- (d) reflexive transitive and symmetric
- (e) none of these

Answer: a

Solution

$$\because N_5 = \{5, 10, 15, 20, 25, 30, 35, \dots\}$$

$$\text{and } N_7 = \{7, 14, 21, 28, \dots\}$$

$$\therefore N_5 \cap N_7 = \{35, 70, \dots\} = N_{35}$$

44. If  $N_a = \{an : n \in N\}$ , then  $N_5 \cap N_7$  is equal to

- (a)  $N_7$
- (b) N
- (c)  $N_{35}$
- (d)  $N_5$
- (e)  $N_{12}$

Answer: c

Solution

$$\because n(A \times B \times C) = n(A) \times n(B) \times n(C)$$

$$\therefore n(C) = \frac{24}{4 \times 3} = 2$$

45. If  $n(A) = 4$ ,  $n(B) = 3$ ,  $n(A \times B \times C) = 24$ , then  $n(C)$  is equal to

- (a) 288
- (b) 1
- (c) 12
- (d) 2

Answer: e

Solution

According to question,

$$2^m - 2^n = 56$$

$$2^n (2^{m-n} - 1) = 56$$

This is possible only, if  $m = 6$  and  $n = 3$

46. Two finite sets have m and n elements respectively. The total number of subsets of first set is 56 more than the total number of subsets of the second set. The values of m and n respectively are

- (a) 7, 6
- (b) 6, 3
- (c) 5, 1
- (d) 7, 8
- (e) 3, 6

Answer: b

Solution

We have,  $f(x) = \sin^{-1}(\log_2 x)$

$$\therefore -1 \leq \log_2 x \leq 1 \quad (\because -1 \leq \sin^{-1} x \leq 1)$$

$$\Rightarrow 2^{-1} \leq x \leq 2^1$$

$$\Rightarrow \frac{1}{2} \leq x \leq 2$$

$$\therefore \text{Domain of the function} = \left\{x : \frac{1}{2} \leq x \leq 2\right\}$$

47. Domain of the function  $f(x) = \sin^{-1}(\log_2 x)$  in a set of real numbers is

- (a)  $\{x : 1 \leq x \leq 2\}$
- (b)  $\{x : 1 \leq x \leq 3\}$
- (c)  $\{x : -1 \leq x \leq 2\}$
- (d)  $\{x : \frac{1}{2} \leq x \leq 2\}$
- (e)  $\{x : -\frac{1}{2} \leq x \leq 2\}$

Answer: d

Solution

According to the given condition  $2^m - 2^n = 48$

This is possible only when  $m = 6$  and  $n = 4$ .

48. Two finite sets have  $m$  and  $n$  elements. The number of elements in the power set of first set is 48 more than the total number of elements in the power set of the second set. Then the values of  $m$  and  $n$  are

- (a) 7, 6
- (b) 6, 3
- (c) 6, 4
- (d) 7, 4
- (e) 3, 7

**Answer:** c

**Solution**

$$\begin{aligned} n(M) &= 100, n(P) = 70, n(C) = 40 \\ n(M \cap P) &= 30, n(M \cap C) = 28, \\ n(P \cap C) &= 23, \text{ and } n(M \cap P \cap C) = 18 \\ \therefore n(M \cap P' \cap C') &= n[M \cap (P \cup C)'] \\ &= n(M) - n[M \cap (P \cup C)] \\ &= n(M) - [n(M \cap P) + n(M \cap C) \\ &\quad - n(M \cap P \cap C)] \\ &= 100 - [30 + 28 - 18] \\ &= 60 \end{aligned}$$

49. A class has 175 students. The following data shows the number of students opting one or more subjects. Mathematics 100, Physics 70, Chemistry 30, Mathematics and Physics 30, Mathematics and Chemistry 28, Physics and chemistry 23, Mathematics, Physics and Chemistry 18. How many students have offered Mathematics alone?

- (a) 35
- (b) 48
- (c) 60
- (d) 22
- (e) 30

**Answer:** c

**Solution**

$R = \{(a, b) : 1 + ab > 0\}$   
It is clear that the given relation on  $S$  is reflexive, symmetric but not transitive.

50. Let  $S$  be the set of all real numbers. Then the relation  $R = \{(a, b) : 1 + ab > 0\}$  on  $S$  is

- (a) reflexive and symmetric but not transitive
- (b) reflexive and transitive but not symmetric
- (c) symmetric and transitive but not reflexive
- (d) reflexive transitive and symmetric
- (e) none of these

**Answer:** a

**Solution**

$$\begin{aligned} \therefore N_5 &= \{5, 10, 15, 20, 25, 30, 35, \dots\} \\ \text{and } N_7 &= \{7, 14, 21, 35, \dots\} \\ \therefore N_5 \cap N_7 &= \{35, 70, \dots\} = N_{35} \end{aligned}$$

51. If  $N_a = \{an : n \in \mathbb{N}\}$ , then  $N_5 \cap N_7$  is equal to

- (a)  $N_7$
- (b)  $N$
- (c)  $N_{35}$
- (d)  $N_5$
- (e)  $N_{12}$

**Answer:** c

**Solution**

$$\begin{aligned} \therefore n(A \times B \times C) &= n(A) \times n(B) \times n(C) \\ \therefore n(C) &= \frac{24}{4 \times 3} = 2 \end{aligned}$$

52. If  $n(A) = 4, n(B) = 3, n(A \times B \times C) = 24$ , then  $n(C)$  is equal to

- (a) 288
- (b) 1
- (c) 12
- (d) 2

**Answer:** d

**Solution**

According to question,

$$2^m - 2^n = 56$$

$$2^n (2^{m-n} - 1) = 56$$

This is possible only, if  $m = 6$  and  $n = 3$

53. Two finite sets have  $m$  and  $n$  elements respectively. The total number of subsets of first set is 56 more than the total number of subsets of the second set. The values of  $m$  and  $n$  respectively are

- (a) 7, 6
- (b) 6, 3
- (c) 5, 1
- (d) 7, 8
- (e) 3, 6

**Answer:** b

**Solution**

The possible sets are  $\{\pm 2, \pm 3\}$  and  $\{\pm 4, \pm 1\}$ ; therefore, number of elements in required set is 8.

54. The number of elements in the set  $\{(a, b) : 2a^2 + 3b^2 = 35, a, b \in \mathbb{Z}\}$ , where  $\mathbb{Z}$  is the set of all integers is

- (a) 2
- (b) 4
- (c) 8
- (d) 12
- (e) 16

**Answer:** c

**Solution**

$$\therefore A = \{2, 3\}, B = \{2, 4\} \text{ and } C = \{4, 5\}$$

$$\therefore B \cap C = \{4\}$$

$$\text{Hence, } A \times (B \cap C) = \{(2, 4), (3, 4)\}$$

55. If  $A = \{x : x^2 - 5x + 6 = 0\}, B = \{2, 4\}, C = \{4, 5\}$  then  $A \times (B \cap C)$  is

- (a)  $\{(2,4), (3,4)\}$
- (b)  $\{(4,2), (4,3)\}$
- (c)  $\{(2,4), (3,4), (4,4)\}$
- (d)  $\{(2,3), (3,3), (4,4)\}$
- (e) null set

**Answer:** a

**Solution**

$$n(C) = 20, n(B) = 50, n(C \cap B) = 10$$

$$\therefore n(C \cup B) = n(C \cup B)$$

$$= n(C) + n(B) - n(C \cap B)$$

$$= 20 + 50 - 10$$

$$= 60 \text{ per cent}$$

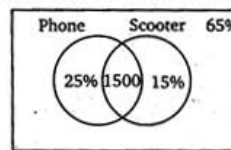
56. In a city 20% of the population travels by car, 50% travels by bus and 10% travels by both car and bus. The persons traveling by bus or car is

- (a) 80%
- (b) 40%
- (c) 60%
- (d) 70%
- (e) 30%

**Answer:** c

**Solution**

Let the total population of town be  $x$ .



$$\therefore \frac{25x}{100} + \frac{15x}{100} - 1500 + \frac{65x}{100} = x$$

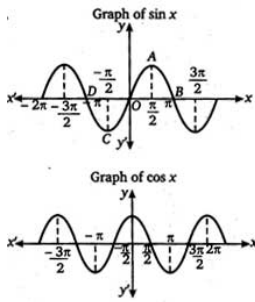
$$\Rightarrow \frac{105x}{100} - x = 1500$$

$$\Rightarrow \frac{5x}{100} = 1500$$

$$\Rightarrow x = 30000$$

57. In a certain town 25% families own a cell phone, 15% families own a scooter and 65% families own neither a cell phone nor a scooter. If 5000 families own both a cell phone and a scooter, then the total number of families in the town is
- 10000
  - 20000
  - 30000
  - 40000
  - 50000

**Answer: c**  
**Solution**



In the given options (a), (b), (c), (e) the curves are decreasing and increasing in the given intervals, so it is not one-to-one function. But in option (d), the curve is only increasing in the given intervals, so it is one-to-one function.

58. Which of the following functions is one to one?
- $f(x) = \sin x, x \in [-\pi, \pi]$
  - $f(x) = \sin x, x \in [-3\pi/2, -\pi/4]$
  - $f(x) = \cos x, x \in [-\pi/2, \pi/2]$
  - $f(x) = \cos x, x \in [\pi, 2\pi]$
  - $f(x) = \cos x, x \in [-\pi/4, \pi/4]$

**Answer: d**  
**Solution**

Given function is  $f(n) = {}^{8-n}P_{n-4}, 4 \leq n \leq 6$ . It is defined, if

- $8 - n > 0 \Rightarrow n < 8$  ... (i)
- $n - 4 \geq 0 \Rightarrow n \geq 4$  ... (ii)
- $n - 4 \leq 8 - n$   
 $\Rightarrow 2n \leq 12 \Rightarrow n \leq 6$  ... (iii)

From Eqs. (i), (ii) and (iii), we get  
 $n = 4, 5, 6$

Hence, range of  $f(n) = \{ {}^4P_0, {}^3P_1, {}^2P_2 \}$   
 $= \{ 1, 3, 2 \}$

59. Let n be the natural number. Then the range of the function  $f(n) = {}^{8-n}P_{n-4}, 4 \leq n \leq 6$  is
- $\{1, 2, 3, 4\}$
  - $\{1, 2, 3, 4, 5, 6\}$
  - $\{1, 2, 3\}$
  - $\{1, 2, 3, 4, 5\}$
  - null

**Answer: c**  
**Solution**

$\because A$  and  $B$  are not disjoint sets .

$\therefore n(A \cup B) = n(A) + n(B) - n(A \cap B)$

60. If A and B are not disjoint sets, then  $n(A \cup B)$  is equal to
- $n(A) + n(B)$
  - $n(A) + n(B) - n(A \cap B)$
  - $n(A) + n(B) + n(A \cap B)$
  - $n(A) n(B)$
  - $n(A) - n(B)$

**Answer: b**